

FOR 240 – Homework Assignment 2
Mathematical Programming in Forest Management with Excel Solver Tool
Introduction to Computing in Natural Resources

In this exercise, we will use Microsoft Excel to solve the following linear programming problem. WVUTIMBER produces both sawlogs and pulpwood from its forest. It takes 600 acres of forest to produce 100 truckloads of sawlogs and 400 acres to produce 100 truckloads of pulpwood. Let's assume that 100 truckloads make one standard delivery. The company has 2400 acres of forest lands. It takes about 100 labor hours to harvest one truckload of sawlogs and 200 hours to produce same amount of pulpwood. The total number of labor hours with the company is 600 for a given harvesting season. It is assumed that the demand of pulpwood at processing industry is not more than 100 truck loads than that of sawlogs. Also, maximum demand of pulpwood is 200 truck loads per season. Let's say that profit from one standard delivery (100 truck loads) of sawlog is \$ 50000 and profit from pulpwood is \$ 40000. WVUTIMBER wants to determine the best combination of sawlogs and pulpwood harvesting from its forest.

This problem can be formulated as LP. Let's define the decision variables first.

X_1 = # of 100 Truckloads of sawlogs per season
 X_2 = # of 100 Truckloads of pulpwood per season

The objective is to maximize the profit (z) of this timber sale including pulpwood and sawlogs.

$$\text{Maximize } z = 50,000X_1 + 40,000X_2$$

Next, we need to define our constraints.

Acres:

Total available acres = 2,400
100 truckloads of sawlogs require 600 acres.
100 truckloads of pulpwood require 400 acres.

Hence, $600X_1 + 400X_2 \leq 2400$ (we can cut all the forest lands or leave some if this is not going to be profitable at present time. But we cannot cut more than what we have.

Labor hours:

Total available labor hours: 600
Sawlogs requirement per 100 truckloads = 100
Pulpwood requirement per 100 truckloads = 200
Hence
 $100X_1 + 200X_2 \leq 600$

Market restriction:

Excess of pulpwood truck load over sawlogs truckloads should be less than 100.

Hence, $X_2 - X_1 \leq 1$

Demand restriction:

Maximum demand of pulpwood is 200 tuckloads.

$X_2 \leq 2$;

As in any LP, the variables cannot be negative, So $X_1, X_2 \geq 0$.

This problem can be written in the following format:

Max: $Z = 50000X_1 + 40000X_2$ (OBJECTIVE FUNCTION)

$600X_1 + 400X_2 \leq 2400$ (CONSTRAINT 1)

$100X_1 + 200X_2 \leq 600$(CONSTRAINT 2)

$X_2 - X_1 \leq 1$ (CONSTRAINT 3)

$X_2 \leq 2$ (CONSTRAINT 4)

$X_1 \geq 0$ (NON NEGATIVE CONSTRAINT)

$X_2 \geq 0$ (NON NEGATIVE CONSTRAINT)

Create an Excel workbook and save it as LP.xlsx, which must include the above model. Once you have this workbook, you need to accomplish the followings:

- a. Solve the model using excel solver.
- b. Report optimal value of Z.
- c. Describe how much sawlogs and pulpwoods should be harvested to obtain the reported value of z.

Please provide me a typed summary report including the output from solver as well as reported values by the beginning of the class next week.